# **Data Representation**

Interpreting bits to give them meaning

Part 2: Hexadecimal and Practical Issues

Notes for CSC 100 - The Beauty and Joy of Computing The University of North Carolina at Greensboro

# **Class Reminders**

Class/Assignments:

Assignment 2 will be handed out today - start planning!

Lab Exercises:

Review Lab 4 solutions (in Blackboard) - important for HW 2!

#### Blown to Bits:

Chapter 2 discussion - contribute before Wednesday (10:00am)

# From Last Time...

Key points from "Data Representation, Part 1":

- A number is an abstract idea
- Anything you can point at or write down is a <u>representation</u> of a number
- Lots of different representations for the same number:
  - Written in decimal notation (what we're most familiar with)
  - Written in roman numerals (e.g., 6 is the same as VI)
  - Written as a set of "tick marks" (e.g., 6 is the same as IIIIII)
     Written in binary (e.g., 6 is the same as 1102)
  - Written in binary (e.g., 6 is the same as 1102)
     As a sequence of voltages on wires
- Computers work with binary because switches are off or on (0 or 1)
- Converting between number bases doesn't change the number, just chooses a different representation

# Hexadecimal - another useful base

<u>Hexadecimal</u> is base 16.

How do we get 16 different digits? Use letters!

Hexadecimal digits (or "hex digits" for short): 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F

#### Counting - now our odometer has 16 digits:

0 <sub>16</sub> (= 0 <sub>10</sub> )	6 <sub>16</sub> (= 6 <sub>10</sub> )	C <sub>16</sub> (= 12 <sub>10</sub> )	12 <sub>16</sub> (= 18 <sub>10</sub> )	•••
$1_{16} (= 1_{10})$	7 <sub>16</sub> (= 7 <sub>10</sub> )	D <sub>16</sub> (= 13 <sub>10</sub> )	1316 (= 1910)	
2 <sub>16</sub> (= 2 <sub>10</sub> )	816 (= 810)	E <sub>16</sub> (= 14 <sub>10</sub> )	14 <sub>16</sub> (= 20 <sub>10</sub> )	
3 <sub>16</sub> (= 3 <sub>10</sub> )	9 <sub>16</sub> (= 9 <sub>10</sub> )	F <sub>16</sub> (= 15 <sub>10</sub> )	15 <sub>16</sub> (= 21 <sub>10</sub> )	
4 <sub>16</sub> (= 4 <sub>10</sub> )	A <sub>16</sub> (= 10 <sub>10</sub> )	10 <sub>16</sub> (= 16 <sub>10</sub> )	16 <sub>16</sub> (= 22 <sub>10</sub> )	
5 <sub>16</sub> (= 5 <sub>10</sub> )	B <sub>16</sub> (= 11 <sub>10</sub> )	11 <sub>16</sub> (= 17 <sub>10</sub> )	17 <sub>16</sub> (= 23 <sub>10</sub> )	

Hexadecimal/Decimal	Conversions
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Conversion process is like binary, but base is 16	Hex Digit List		
<u>Problem 1</u> : Convert 423 <sub>10</sub> to hexadecimal: 423/16 = quotient 26, remainder 7 $(=7_{ig})$ 26/16 = quotient 1, remainder 10 $(=A_{ig})$ 1/16 = quotient 0, remainder 1 $(=1_{ig})$	$0_{16} = 0_{10}$ $1_{16} = 2_{10}$ $3_{16} = 3_{10}$ $4_{16} = 4_{10}$ $5_{16} = 5_{10}$ $6_{16} = 6_{10}$		
• Reading digits bottom-up: 423 <sub>10</sub> = 1A7 <sub>16</sub>	$7_{16} = 7_{10}$ $8_{16} = 8_{10}$ $9_{16} = 9_{10}$		
<u>Problem 2</u> : Convert 9C3, <sub>8</sub> to decimal: Start with first digit, 9 9*16 + 12 = 156 156*16 + 3 = 2499	$A_{16} = 10_{10}^{5}$ $B_{16}^{16} = 11_{10}^{10}$ $C_{16}^{16} = 12_{10}^{10}$ $D_{16}^{16} = 13_{10}^{10}$ $E_{16}^{16} = 14_{10}^{10}$ $F_{16} = 15_{10}^{10}$		
• Therefore, 9C3 <sub>16</sub> = 2499 <sub>10</sub>	16 10		

#### **Hexadecimal/Decimal Conversions** Hex Digit List Conversion process is like binary, but base is 16 $\begin{array}{l} 0_{16}=0_{10}\\ 1_{16}=2_{10}\\ 2_{16}=2_{10}\\ 3_{16}=3_{10}\\ 4_{16}=5_{10}\\ 6_{16}=6_{10}\\ 7_{16}=7_{10}\\ 9_{16}=9_{10}\\ A_{16}=10_{10}\\ B_{16}=12_{10}\\ D_{16}=12_{10}\\ D_{16}=14_{10}\\ E_{16}=14_{10}\\ \end{array}$ $\begin{array}{l} \underline{Problem 1}: \mbox{ Convert 423}_{10} \mbox{ to hexadecimal:} \\ 423/16 = \mbox{quotient 26, remainder 7 (=7, _{16})} \\ 26/16 = \mbox{quotient 1, remainder 10 (=} \mbox{$1_{16}$}) \\ 1/16 = \mbox{quotient 0, remainder 1 (=} \mbox{$1_{16}$}) \end{array}$ • Reading digits bottom-up: 423<sub>10</sub> = 1A7<sub>16</sub> Your turn! Convert: <u>Problem 2</u>: Convert 9C3<sub>16</sub> to decimal: Start with first digit, 9 9\*16 + 12 = 156 103<sub>10</sub> = \_\_\_\_ 247<sub>10</sub> = \_\_\_\_ 952<sub>10</sub> = \_\_\_ 16 - 16 - 16 156\*16 + 3 = 2499 15,10 3C<sub>16</sub> = \_\_\_ B9<sub>16</sub> = \_\_\_ 357<sub>16</sub> = \_\_\_ • Therefore, 9C3<sub>16</sub> = 2499<sub>10</sub> - 10 - 10 - 10











## Use of hexadecimal in file dumps

Binary is a very long format (8 bits per byte), but often data files only make sense as binary data. Hexadecimal is great for this - simple one-to-one correspondence with binary, and more compact.

Sample	"file	dump'	

inple	me uump									
	0000000:	ffd8	ffel	35fe	4578	6966	0000	4949	2a00	5.ExifII*.
	0000010:	0800	0000	0b00	0e01	0200	2000	0000	9200	
	0000020:	0000	0f01	0200	0600	0000	b200	0000	1001	
	0000030:	0200	1900	0000	b800	0000	1201	0300	0100	
	0000040:	0000	0600	0000	1a01	0500	0100	0000	d800	
	0000050:	0000	1b01	0500	0100	0000	e000	0000	2801	
	0000060:	0300	0100	0000	0200	0000	3201	0200	1400	
	0000070:	0000	e800	0000	1302	0300	0100	0000	0200	
	0000080:	0000	6987	0400	0100	0000	fc00	0000	2588	i%.
	0000090:	0400	0100	0000	2413	0000	£213	0000	2020	\$
	00000a0:	2020	2020	2020	2020	2020	2020	2020	2020	
	00000b0:	2020	2020	2020	2020	2020	2020	2000	4361	.Ca
	00000c0:	6e6f	6e00	4361	6e6f	6e20	506f	7765	7253	non.Canon PowerS
	00000d0:	686f	7420	5358	3233	3020	4853	0000	0000	hot SX230 HS
	00000e0:	0000	0000	b400	0000	0100	0000	b400	0000	
	00000f0:	0100	0000	3230	3131	3a30	373a	3134	2031	2011:07:14 1
	0000100:	353a	3039	3a32	3700	2100	9a82	0500	0100	5:09:27.!
	0000110:	0000	8e02	0000	9d82	0500	0100	0000	9602	
	0000120:	0000	2788	0300	0100	0000	6400	0000	3088	'd0.
Po	sition in file	Actu	al bina	ary da	ta (wr	itten ir	n hexa	decin	nal)	The same data, showing
										character representation



# Remember....

Don't get lost in the details and manipulations:

Any base is a representation of an abstract number

We are interested in working with the number, and computations are not "in a base" - the base is only useful for having it make sense to us or the computer

## **Practice!**

You should be able to convert from one base to another.

Lots of ways to practice:

- By hand: Pick a random number convert to binary and convert back did you get the same value?
- This isn't foolproof: You could have made two mistakes!
- With a calculator: Many calculators (physical and software) do base conversion check your randomly selected conversions.
- With a web site: Several web sites provide says to practice
   o For example, see <a href="http://cs.iupui.edu/~aharris/230/binPractice.html">http://cs.iupui.edu/~aharris/230/binPractice.html</a>

# **Practical Issues with Numbers**

Finite Length Integers

Question (a little contrived):

If a CPU has 4 single-bit storage locations for each number, what happens when you add:

1111<sub>2</sub> + 0001<sub>2</sub> = \_\_\_\_\_ 2

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Answer Part 1: If you did this on paper, you'd get 10000,

Which leads to another question:

How do we store 5 bits when there are only storage locations for 4 bits?

#### **Practical Issues with Numbers** Finite Length Integers

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Which leads to another question:

How do we store 5 bits when there are only storage locations for 4 bits?

<u>Answer Part 2</u>: What CPUs do is throw out the 5th bit, storing  $0000_2$ Which means: To a 4-bit computer, 15 + 1 = 0

# **Practical Issues with Numbers**

Finite Length Integers

On real computers:

- This happens, but with 32-bit numbers or 64-bit numbers instead of 4.
- When things "wrap around" it actually goes to negative values ... On a 32-bit CPU: 2,147,483,647 + 1 = -2,147,483,648

However: Some programming languages/systems support numbers larger than the hardware, by using multiple memory locations.

Let's try this!





#### **Practical Issues with Numbers** Finite Length Integers In C: In Java: In Python: int val=1000\*1000\*1000\*1000; printf("%d\n", val); int val = 1000\*1000\*1000\*1000; System.out.println(val); x = 1000\*1000\*1000\*1000 print x Outputs: Outputs: Outputs: -727379968 -727379968 1000000000000 First thought: Python is cool! Second thought: Don't expect something for nothing... Let's do something pretty useless (that takes a lot of integer operations) Problem: Compute the last 6 digits of the billionth Fibonacci number





# **Practical Issues with Numbers**

Finite Precision Floating Point

Question: How do you write out 1/3 in decimal?

Answer: 0.333333333333....

Observation: Impossible to write out exactly with a finite number of digits

The same holds in binary!

Can be written exactly
$0.5 = 0.1_2$ $0.25 = 0.01_2$ $0.375 = 0.011_2$

Can<u>not</u> be written exactly <sup>1</sup>/<sub>3</sub> = 0.0101010101...<sub>2</sub> <sup>1</sup>/<sub>4</sub> = 0.001100110011...<sub>2</sub> 1/10 = 0.0001100110011...<sub>2</sub>

Imagine: How hard is it to write banking software when there is no finite representation of a dime (0.10 dollars)?!?!?

Solutions people came up with:

Work with cents (integers!) or special codings (BCD=Binary Coded Decimal)



### **Still More Data Representation for Later**

Now we know all about representing numbers

But computers also deal with text, web pages, pictures, sound/music, video, ...

How does that work?