# **Algorithms**

Part 3: Time Complexity Basics
Constant, Linear, and Quadratic Time

Notes for CSC 100 - The Beauty and Joy of Computing The University of North Carolina at Greensboro

### Reminders

### Readings:

Emma - contribute to on-line discussion by Monday!

### Homework:

Homework 2 due on Wednesday

On the horizon: Midterm on Wednesday, Oct. 4

## **Constant time**

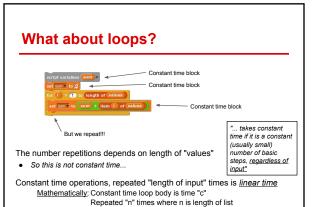
We say a script (or part of a script or block definition) takes *constant time* if it is a constant (usually small) number of basic steps, regardless of input.

Question: Are all of these constant time?

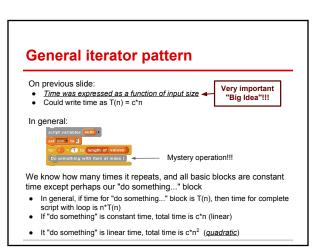




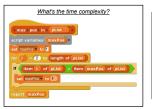




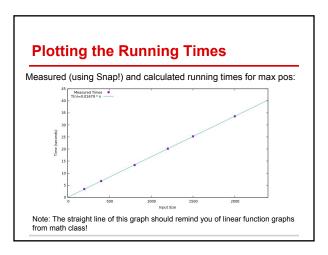
Total time is then c\*n (that's a linear function!)



# Two challenges







# Plotting the Running Times Measured (using Snap!) and calculated running times for sort:

# 

# **Predicting Program Times - Linear** Basic idea: Given time complexity and sample time(s) can estimate time on larger inputs Linear time: When input size doubles, time doubles When input size triples, time triples When input size goes up by a factor of 10, so does time Example: A linear time algorithm runs in 10 sec on input size 10,000 How long to run on input size 1,000,000? Answer: 1,000,000 / 10,000 = 100 times larger input Therefore 100 times larger time, or 10 \* 100 = 1,000 sec Or 1,000 / 60 = 16.667 minutes **Predicting Program Times - Quadratic** Basic idea: Given time complexity and sample time(s) can estimate time on larger inputs Quadratic time: When input size doubles (2x), time quadruples (4x) Input size goes up by a factor of 10, time goes up 10<sup>2</sup>=100 times Input size goes up k times, time goes up $k^2$ times Example: A quadratic time algorithm runs in 10 sec on input size 10,000 How long to run on input size 1,000,000? Answer: 1,000,000 / 10,000 = 100 times larger input Therefore $100^2 = 10,000$ times larger time, or 100,000 sec Or 100,000 / 60 = 1666.7 minutes (or 27.8 hours) **Predicting Program Times - Your Turn** Joe and Mary have created programs to analyze crime statistics, where the input is some data on each resident of a town Joe's algorithm is quadratic time Mary's algorithm is linear time Both algorithms take about 1 minute for a town of size 1000 Both would like to sell their program to the City of Greensboro (population 275,000)

<u>Problem</u>: Estimate how long each program would take to run for Greensboro

# **Summary**

- Algorithm "time complexity" is in basic steps
- Common complexities from this lecture, from fastest to slowest are constant, linear, and quadratic
  - o A single step, or sequence of constant-time blocks is constant time
  - A simple loop with constant time operations repeated is linear time
  - A loop containing a linear time loop is quadratic
- Speed depends on algorithm time complexity
  - o Constant time is great, but not many interesting things are constant time
  - Linear time is very goodQuadratic time is OK
- Given time complexity and one actual time, can estimate time for larger inputs