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# CSC 580

## Cryptography and Computer Security

*Random Bit Generators*  
*(Sections 8.1-8.3)*

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February 23, 2017

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## Overview

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Today:

- HW 5 quiz
- Pseudorandom generation - concepts and simple techniques

To do before Thursday:

- Do HW 6
  - Read "Security Models" handout
  - Finish project phase 2 - report submitted in class, code in BitBucket
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## What do we mean by "randomness"?

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Common perception - random physical events

- Flipping a coin
- Rolling a die
- Blind draw from a bag



Some properties:

- Statistically uniform
  - Non-uniform randomness is possible, but less interesting in crypto
- Independence
- Unpredictability (next numbers can't be guessed)

Key concept: Entropy

- Measures amount of randomness from a random source
  - Example 1: 64 true random bits has 64-bit of entropy
  - Example 2: English language entropy is about 2-bits per letter
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## Random Number Generators

Delivers an unbounded-length sequence (stream)

TRNG - True Random Number Generator

- Sometimes called NRBG (non-deterministic random bit generator)
- Based on physical randomness
- OS can gather physical randomness - disk timing, mouse moves, ...
  - `/dev/random` in Linux - **blocking** random source
- Can also be special-purpose device (noisy diode,... even a lava lamp)

PRNG - Pseudo Random Number Generator

- Sometimes called DRBG (deterministic random bit generator)
- Sequence computed from a **seed**
- Consumer of stream typically doesn't know seed
- Computing again with same seed gives same sequence (repeatable)

TRNG/PRNG hybrids

- True randomness "mixed in" to pseudorandom generator
- `/dev/urandom` in Linux - **non-blocking** random source

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## Some applications and properties

What properties are needed in different applications?

Application	Good Statistics	Unpredictable (fwd)	Repeatable
Random simulation	Must have	No need	Depends
Nonce	Must have	Must have	No need
Stream cipher	Must have	Must have	Must have

Observations

- Cannot use a TRNG for a stream cipher (can for others)
- All applications need good statistical properties (uniformity, independence)
- In crypto applications, unpredictability is important

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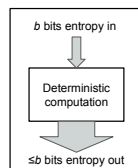
## A warning when thinking about PRNGs

If numbers are computed, they aren't random!

*Anyone who considers arithmetical methods of producing random digits is, of course, in a state of sin. For, as has been pointed out several times, there is no such thing as a random number — there are only methods to produce random numbers, and a strict arithmetic procedure of course is not such a method. - John von Neumann, 1951*

Computation cannot increase entropy

- 1000 bits output from a PRNG with 16-bit seed has at most 16 bits of entropy!



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## Good PRNG Importance

Security often fails just because of bad PRNG use

Can fail because of either:

- Bad seeding (not random or not large enough)
- Bad algorithm

Example 1: The original SSL implementation (Netscape Navigator)

- Seeded with process id (15 bits) and current time (a few bits or uncertainty)
- Made cryptographic keys guessable - completely destroyed security

Example 2: Bad algorithm in NIST standards - Dual EC DRBG

- Exposed as a possible backdoor after Snowden leaks

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## Dual EC DRBG

The potential backdoor is exposed

The screenshot shows a New York Times article from September 16, 2013. The headline is "Government Announces Steps to Restore Confidence on Encryption Standards". The sub-headline reads: "SAN FRANCISCO — The federal agency charged with recommending cybersecurity standards said Tuesday that it would reopen the public online process for an encryption standard after reports that the National Security Agency had written the standard and could break it." A red circle highlights the sub-headline. Below the headline, there is a quote: "We want to assure the IT, cybersecurity community that the transparent, public process used to rigorously vet our standards is still in place." The article also mentions that the NSA had inserted a backdoor into a 2006 standard adopted by NIST and later by the International Organization for Standardization.

People have always worried about NSA backdoors - this one appears to have been real!

Was adopted by NIST as a standard.

Withdrawn from standard after discoveries

But... Dual EC DRBG is super-slow anyway - surely no one uses it... right?

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## Dual EC DRBG

Oops - people DID use it - maybe even unknowingly!

The screenshot shows an RSA Security advisory. The headline is "RSA TELLS ITS DEVELOPER CUSTOMERS: STOP USING NSA-LINKED ALGORITHM". Below the headline is the RSA BSAFE logo. The advisory text states that RSA Security has released an advisory to developer customers today, noting that the algorithm is the default in one of its toolkits and strongly advising them to stop using the algorithm. It also provides information on how to change the default to one of a number of other algorithms.

Not only used, but was the default DRBG in RSA's BSAFE library!

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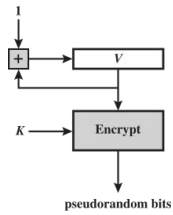
## Fast PRNG from a block cipher

Widely-used technique: CTR mode

- Key and initial counter are seed
- Basically the XOR pad from CTR mode (ignoring plaintext)

Key property: If AES-CTR mode is a secure encryption scheme (technically, is IND-CPA secure) then this is a secure PRNG

To think about: If  $K$  is fixed and secret (embedded in hardware) and only  $V$  is the seed, can it be "backdoored" (HW problem)



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